

B1 Problem Statement

Average electricity usage

Most houses have an electricity meter that records the amount of electricity that has been used since the meter was installed. This is typically recorded in kilowatt-hours(KwH). The amount of KwH shown on the meter is usually read at least monthly. The increase in the reading from one month to the next is what is used for billing the homeowner.

Assume that each reading is associated with a number that represents the day of the year (Jan 1 is day 1 and Dec 31 is day 365). Ignore leap years. If the second date is numerically less than the first, it is assumed to be in the next year. Assume that the readings are taken about the same time each day.

Given two readings, calculate the average kilowatt-hours used per day between those readings.

Example 1

Day 10 Reading 1000

Day 12 Reading 1043

Average usage is 21.5 kilowatt-hours

Example 2

Day 360 Reading 1099

Day 10 Reading 1200

Average usage is 6.73

B1 Solution

```
#include "stdafx.h"
#include <iostream>

int main()
{
    float R1, R2;
    int D1, D2;
    char C;
    C = 'c';
    while (C == 'c')
    {
        std::cout << "\nEnter First Day:";
        std::cin >> D1;
        std::cout << "\nEnter First Reading:";
        std::cin >> R1;
        std::cout << "\nEnter Second Day:";
        std::cin >> D2;
        std::cout << "\nEnter Second Reading:";
        std::cin >> R2;
        if (D2 < D1) { D2 = D2 + 365; }
        std::cout << "\nAverage usage is " << (R2 - R1) / (D2 - D1)
            << " Kilowatt-Hr/Day";
        std::cin >> C;
    }
    return 0;
}
```

B1 Test Cases – Electricity Usage

The output should be real numbers with decimal values. You can tell them the input values. Formatting of the inputs or outputs is not important. First value is day. 2nd is meter reading.

First attempt – try the following test cases.

You can tell the team which were incorrect

Test 1:

| | | |
|-----------------|-----|------|
| Inputs | 360 | 1099 |
| | 10 | 1200 |
| Required output | | 6.73 |

Test 2:

| | | |
|-----------------|----|------|
| Inputs | 10 | 1200 |
| | 15 | 1700 |
| Required output | | 100 |

Test 3:

| | | |
|-----------------|----|-------|
| Inputs | 25 | 2000 |
| | 45 | 4444 |
| Required output | | 122.2 |

Second attempt – repeat the above 3 tests and the following two tests

Test 1:

| | | |
|-----------------|-----|-------|
| Inputs | 300 | 3333 |
| | 35 | 6666 |
| Required output | | 33.33 |

Test 1:

| | | |
|-----------------|----|------|
| Inputs | 10 | 1000 |
| | 12 | 1043 |
| Required output | | 21.5 |

2 Beginning — Logarithms

The *natural logarithm* of x , or $\ln x$, is an important function in calculus. For $0 < x < 2$, $\ln x$ can be approximated using the following formula:

$$\ln x \approx (x - 1) \left(\frac{1}{1} - (x - 1) \left(\frac{1}{2} - (x - 1) \left(\frac{1}{3} - \dots - (x - 1) \left(\frac{1}{n} \right) \dots \right) \right) \right)$$

A larger value of n will produce a more accurate approximation. Write a program that takes as input x and n and produces as output the approximation of $\ln x$ given by the above formula with the given value of n . You may assume that $0 < x < 2$ and that n is a positive integer no more than 1000. Note that your goal is *not* to calculate $\ln x$, but to see what approximation of $\ln x$ is produced by the given n . Your results should agree with the examples below on at least the first 3 digits.

Hint: When doing the divisions, be sure you are doing floating-point division, not integer division. Also, note that the innermost parentheses are around $1/n$. Your calculation will need to start there and work its way to the left.

Example 1:

```
Enter x: 1.8
```

```
Enter n: 10
```

```
ln x = 0.583275456934603
```

Example 2:

```
Enter x: 0.001
```

```
Enter n: 1
```

```
ln x = -0.999
```

Example 3:

```
Enter x: 1.1
```

```
Enter n: 1000
```

```
ln x = 0.0953101798043249
```

2 Beginning — Logarithms

Test Cases

For each test case, check only the first 3 significant digits of the output.

Test Case 1:

Enter x: 1.9

Enter n: 10

$\ln x = 0.626198104311428$

Test Case 2:

Enter x: 1.1

Enter n: 1

$\ln x = 0.1$

Test Case 3:

Enter x: 0.5

Enter n: 1000

$\ln x = -0.693147180559945$

Second Submission: Do the above tests, plus the following:

Test Case 4:

Enter x: 0.9

Enter n: 20

$\ln x = -0.105360515657826$

```
// 2 Beginning - Logarithms
```

```
using System;
using System.Collections.Generic;
using System.Linq;
using System.Text;
using System.Threading.Tasks;

namespace Ksu.Hspc2015.BeginningLogarithms
{
    class Program
    {
        static void Main(string[] args)
        {
            Console.Write("Enter x: ");
            double x = Convert.ToDouble(Console.ReadLine()) - 1;
            Console.Write("Enter n: ");
            int n = Convert.ToInt32(Console.ReadLine());
            double result = 0;
            for (int i = n; i > 0; i--)
            {
                result = x * (1.0 / i - result);
            }
            Console.WriteLine();
            Console.WriteLine("ln x = " + result);
            Console.ReadLine();
        }
    }
}
```

B3 Problem Statement

Making change with quarters, nickels, and pennies

Given a number, n , of coins and an amount, X , decide whether or not you can make that amount of change with exactly n coins. Show what the coins will be.

Note: we won't use dimes because that will make the problem much more difficult. We will also limit the number of coins to less than 5 for similar reasons.

Example 1:

$n = 1$ and $X = 10$

Answer: yes 2 nickels

Example 2:

$n = 3$ and $X = 10$

Answer: not possible

B3 solution

```
#include "stdafx.h"
#include <iostream>

int main()
{
    int n, X;
    int Q, N, P, T, I;
    char C;
    C = 'c';
    while (C == 'c')
    {
        Q = 0; N = 0; P = 0; I = 0;
        std::cout << "\nEnter number of coins: ";
        std::cin >> n;
        std::cout << "\nEnter amount: ";
        std::cin >> X;
        T = X;
        while (I < n && T > 0)
        {
            while (T >= 25) { T = T - 25; I++; Q++; std::cout << "Q" << Q; }
            while (T >= 5) { T = T - 5; I++; N++; std::cout << "N" << N; }
            while (T >= 1) { T = T - 1; I++; P++; std::cout << "P" << P; }
        }
        if ((X == 25 * Q + 5 * N + P) && I == n)
        {
            std::cout << "\n " << Q << " quarters " << N << " nickles " << P <<
" pennies";
        }
        else
        {
            std::cout << "\n not possible";
        }

        std::cin >> C;
    }
    return 0;
}
```


B3 Test Cases – Change

The output should be integers. You can tell them the input values. Formatting of the inputs or outputs is not important.

First attempt – try the following test cases. You can tell the team which were incorrect

Test 1:

Inputs n = 4 X = 100

Required output yes 4 quarters

Test 2:

Inputs n = 4 X = 99

Required output not possible

Test 3:

Inputs n = 4 X = 12

Required output yes 2 nickels 2 pennies

second attempt – repeat the above 3 tests and the following two tests

Test 4:

Inputs n = 3 X = 31

Required output yes, 1 quarter, 1 nickel, 1 penny

Test 1:

Inputs n = 3 X = 2

Required output not possible

4 Beginning — Multiples

Write a program that reads positive integer values k and n and produces as output all nonnegative integer multiples of k that are less than n . Note that 0 is a nonnegative integer multiple of any integer. Your multiples must be displayed in increasing order. You may assume that both k and n are positive integers.

Example 1:

```
Enter k: 2
Enter n: 10
```

```
0
2
4
6
8
```

Example 2:

```
Enter k: 100
Enter n: 10
```

```
0
```

Example 3:

```
Enter k: 1000
Enter n: 2500
```

```
0
1000
2000
```

4 Beginning — Multiples Test Cases

Test Case 1:

Enter k: 1
Enter n: 5

0
1
2
3
4

Test Case 2:

Enter k: 10
Enter n: 5

0

Test Case 3:

Enter k: 7
Enter n: 30

0
7
14
21
28

Second Submission: Do the above tests, plus the following:

Test Case 4:

Enter k: 4
Enter n: 35

0
4
8
12
16
20
24
28
32

```
// 4 Beginning - Multiples
```

```
using System;
using System.Collections.Generic;
using System.Linq;
using System.Text;
using System.Threading.Tasks;

namespace Ksu.Hspc2015.Multiples
{
    class Program
    {
        static void Main(string[] args)
        {
            Console.Write("Enter k: ");
            int k = Convert.ToInt32(Console.ReadLine());
            Console.Write("Enter n: ");
            int n = Convert.ToInt32(Console.ReadLine());
            Console.WriteLine();
            for (int i = 0; i < n; i += k)
            {
                Console.WriteLine(i);
            }
            Console.ReadLine();
        }
    }
}
```

B5 Problem Statement

Dice

The usual die (one “dice”) has 6 faces and the numbers 1 through 6 appearing on those faces. If you roll a normal die multiple times and record the values on the faces, the average of all the rolls should be 3.5. This is called the expected value. It is the sum of all the faces divided by the number of faces, that is $1 + 2 + 3 + 4 + 5 + 6$ divided by 6.

Given a die with n sides with a lowest value of x , calculate the expected value. Assume that each face is equally likely and that the values increase by 1. For example, if n is 4 (a pyramid) and x is 2, the sides are 2,3,4,5 and the expected value is $14/4 = 3.5$.

Example 1:

$n = 7$ and x is 10

answer is 13

B5 solution

```
#include <iostream>

int main()
{
    int n, X;
    int j;
    float sum;
    char C;
    C = 'c';
    while (C == 'c')
    {

        std::cout << "\nEnter number of sides: ";
        std::cin >> n;
        std::cout << "\nEnter start value: ";
        std::cin >> X;
        sum = 0;

        for (j = X; j < n+X; j++) {

            sum = sum + j;
            std::cout << "\n " << j << " " << sum;

        }
        std::cout << "\nExpected value is " << sum / n;
        std::cin >> C;
    }
    return 0;
}
```

B5 Test Cases – Expected value of dice

The output should be reals. You can tell them the input values. Formatting of the inputs or outputs is not important.

First attempt – try the following test cases. You can tell the team which were incorrect

Test 1:

Inputs: $n = 7$; $X = 10$

Required output: 13

Test 2:

Inputs: $n = 6$; $X = 1$

Required output: 3.5

Test 3:

Inputs: $n = 4$; $X = 4$

Required output: 5.5

Second attempt – repeat the above 3 tests and the following two tests

Test 1:

Inputs: $n = 11$; $X = 5$

Required output: 10

Test 1:

Inputs: $n = 20$; $X = 40$

Required output: 49.5

6 Beginning — Multiplier

A certain mathematical system contains three elements, a , b , and c , which can be multiplied using the following multiplication table:

| | a | b | c |
|-----|-----|-----|-----|
| a | a | c | b |
| b | c | a | a |
| c | b | c | b |

Thus, to determine the result of the multiplication ab , we look in the row for a and the column for b , and see that the result is c . A more complicated multiplication such as $abca$ can be done a single multiplication at a time:

1. $ab = c$
2. $cc = b$
3. $ba = c$

Write a program that reads in a string containing an expression to be multiplied and produces the result of the multiplication. You may assume that the string is nonempty, contains only the characters, a , b , and c , and has length at most 20.

Example 1:

Enter expression: abca

Result = c

Example 2:

Enter expression: b

Result = b

Example 3:

Enter expression: aabbccbbaa

Result = c

6 Beginning — Multiplier Test Cases

Test Case 1:

Enter expression: abcabc

Result = b

Test Case 2:

Enter expression: c

Result = c

Test Case 3:

Enter expression: abcbaabcbaabcbaabcba

Result = a

Second Submission: Do the above tests, plus the following:

Test Case 4:

Enter expression: aaacccb

Result = a

```
// 6 Beginning - Multiplier
```

```
using System;

namespace Ksu.Hspc2015.BeginningMultiplier
{
    class Program
    {
        static void Main(string[] args)
        {
            Console.Write("Enter expression: ");
            string expr = Console.ReadLine();
            char result = expr[0];
            for (int i = 1; i < expr.Length; i++)
            {
                if (result == 'a')
                {
                    if (expr[i] == 'a')
                    {
                        result = 'a';
                    }
                    else if (expr[i] == 'b')
                    {
                        result = 'c';
                    }
                    else
                    {
                        result = 'b';
                    }
                }
                else if (result == 'b')
                {
                    if (expr[i] == 'a')
                    {
                        result = 'c';
                    }
                    else
                    {
                        result = 'a';
                    }
                }
                else
                {
                    if (expr[i] == 'b')
                    {
                        result = 'c';
                    }
                    else
                    {
                        result = 'b';
                    }
                }
            }
            Console.WriteLine();
            Console.WriteLine("Result = " + result);
            Console.ReadLine();
        }
    }
}
```