

Neural-Symbolic Integration and Ontologies



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Some Background

**Workshop Series on Neural-Symbolic Learning and Reasoning, since 2005.
Joint with Artur d'Avila Garcez.**

<http://neural-symbolic.org/>

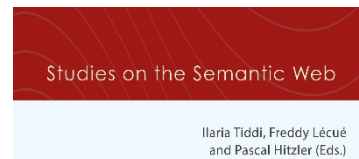
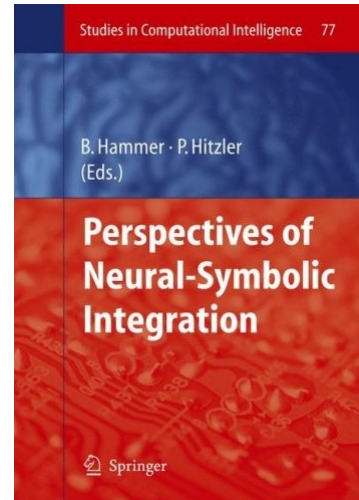
**Barbara Hammer and Pascal Hitzler (eds), Perspectives of
Neural-Symbolic Integration, Springer, 2007**

Neural-Symbolic Learning and Reasoning: A Survey and Interpretation

**Tarek R. Besold, Artur d'Avila Garcez, Sebastian Bader,
Howard Bowman, Pedro Domingos, Pascal Hitzler,
Kai-Uwe Kuehnberger, Luis C. Lamb, Daniel Lowd,
Priscila Machado Vieira Lima, Leo de Penning, Gadi Pinkas,
Hoifung Poon, Gerson Zaverucha**

<https://arxiv.org/abs/1711.03902> (2017)

**Ilaria Tiddi, Freddy Lecue, Pascal Hitzler (eds.), Knowledge Graphs
for eXplainable Artificial Intelligence: Foundations, Applications and
Challenges. Studies on the Semantic Web Vol. 47, IOS Press, 2020.**



Neural-Symbolic Integration and the Semantic Web

Pascal Hitzler, Federico Bianchi, Monireh Ebrahimi, Md Kamruzzaman Sarker,
Neural-Symbolic Integration and the Semantic Web.
Semantic Web 11 (1), 2020, 3-11.

Part 1: Deep Deductive Reasoners

Part 2: Explainable AI using Knowledge Graphs

Deep Deductive Reasoners

Monireh Ebrahimi, Aaron Eberhart, Federico Bianchi, Pascal Hitzler,
Towards Bridging the Neuro-Symbolic Gap: Deep Deductive Reasoners.
Applied Intelligence, 2021, to appear.

Pascal Hitzler, Frank van Harmelen
A reasonable Semantic Web.
Semantic Web 1 (1-2), 39-44, 2010.

Deep Deductive Reasoners



- We trained deep learning systems to do deductive reasoning.
- Why is this interesting?
 - For dealing with **noisy data** (where symbolic reasoners do very poorly).
 - For **speed**, as symbolic algorithms are of very high complexity.
 - Out of **principle** because we want to learn about the capabilities of deep learning for complicated cognitive tasks.
 - To perhaps begin to understand how our (neural) brains can learn to do highly symbolic tasks like formal logical reasoning, or in more generality, mathematics.
A fundamental quest in **Cognitive Science**.

Reasoning as Classification



- **Given a set of logical formulas (a theory).**
- **Any formula expressible over the same language is either**
 - a logical consequence or
 - not a logical consequence.
- **This can be understood as a classification problem for machine learning.**
- **It turns out to be a really hard machine learning problem.**

Knowledge Materialization



- Given a set of logical formulas (a theory).
- Produce all logical consequences **under certain constraints**.
- Without **the qualifier** this is in general not possible as the set of all logical consequences is infinite.
- So we have to **constrain** to consequences of, e.g., a certain syntactic form. For relatively simple logics, this is often reasonably possible.

Deep Reasoners Overview



1. **RDFS via Memory Networks (classification).**
2. **RDFS via Pointer Networks (generative).**
3. **OWL EL via LSTMs (generative)**
4. **LTNs for first-order predicate logic**

Monireh Ebrahimi, Aaron Eberhart, Federico Bianchi, Pascal Hitzler, Towards Bridging the Neuro-Symbolic Gap: Deep Deductive Reasoners. Applied Intelligence, 2021, to appear.

RDFS Reasoning using Memory Networks

Monireh Ebrahimi, Md Kamruzzaman Sarker, Federico Bianchi, Ning Xie, Aaron Eberhart, Derek Doran, Hyeongsik Kim, Pascal Hitzler, Neuro-Symbolic Deductive Reasoning for Cross-Knowledge Graph Entailment. In: Proc. AAAI-MAKE 2021.

additional analysis by Sulogna Chowdhury, Aaron Eberhart and Brayden Pankaskie

RDF reasoning



- **[Note: RDF is one of the simplest useful knowledge representation languages that is not propositional.]**
- **Think knowledge graph.**
- **Think node-edge-node triples such as**

BarackObama	rdf:type	President
BarackObama	husbandOf	MichelleObama
President	rdfs:subClassOf	Human
husbandOf	rdfs:subPropertyOf	spouseOf
- **Then there is a (fixed, small) set of inference rules, such as**
rdf:type(x,y) AND rdfs:subClassOf(y,z) THEN rdf:type(x,z)

Representation

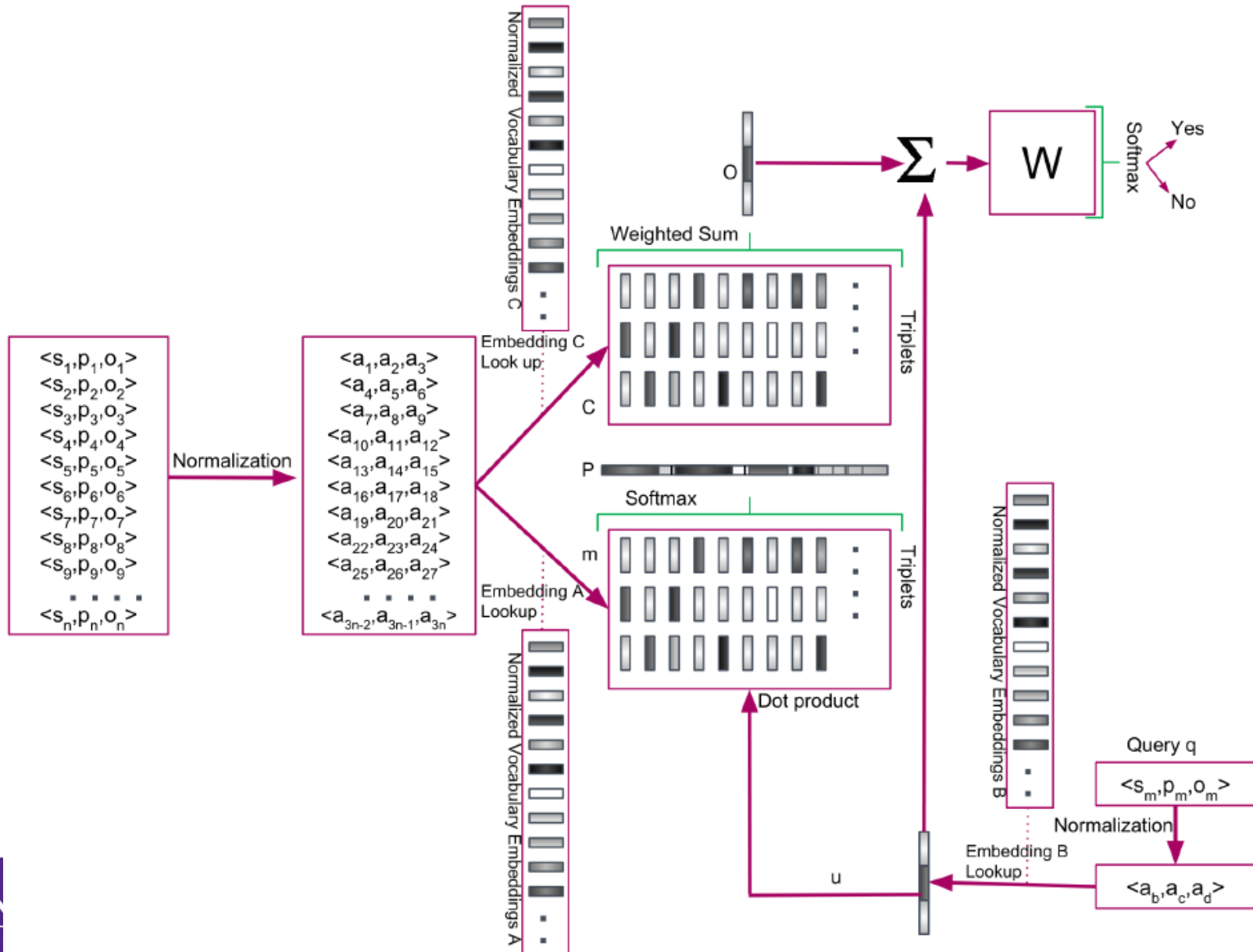
- Goal is to be able to reason over **unseen** knowledge graphs. I.e. the out-of-vocabulary problem needs addressing.
- Normalization of vocabulary (i.e., it becomes shared vocabulary across all input knowledge graphs).
- One vocabulary item becomes a one-hot vector (dimension d , number of normalized vocabulary terms)
- One triple becomes a $3 \times d$ matrix.
- The knowledge graph becomes an $n \times 3 \times d$ tensor (n is the number of knowledge graph triples)
- Knowledge graph is stored in “memory”





- **An attention mechanism retrieves memory slots useful for finding the correct answer to a query.**
- **These are combined with the query and run through a (learned) matrix to retrieve a new (processed) query.**
- **This is repeated (in our experiment with 10 “hops”).**
- **The final out put is a yes/no answer to the query.**

Memory Network based on MemN2N



Experiments: Performance



Test Dataset	#KG	Base						Inferred						Invalid
		#Facts	#Ent.	%Class	%Indv	%R.	%Axiom.	#Facts	#Ent.	%Class	%Indv	%R.	%Axiom.	#Facts
OWL-Centric	2464	996	832	14	19	3	0	494	832	14	0.01	1	20	462
Linked Data	20527	999	787	3	22	5	0	124	787	3	0.006	1	85	124
OWL-Centric Test Set	21	622	400	36	41	3	0	837	400	36	3	1	12	476
Synthetic Data	2	752	506	52	0	1	0	126356	506	52	0	1	0.07	700

Table 2: Statistics of various datasets used in experiments

Baseline: non-normalized embeddings, same architecture

Training Dataset	Test Dataset	Valid Triples Class			Invalid Triples Class			Accuracy
		Precision	Recall /Sensitivity	F-measure	Precision	Recall /Specificity	F-measure	
OWL-Centric Dataset	Linked Data	93	98	96	98	93	95	96
OWL-Centric Dataset (90%)	OWL-Centric Dataset (10%)	88	91	89	90	88	89	90
OWL-Centric Dataset	OWL-Centric Test Set ^b	79	62	68	70	84	76	69
OWL-Centric Dataset	Synthetic Data	65	49	40	52	54	42	52
OWL-Centric Dataset	Linked Data ^a	54	98	70	91	16	27	86
OWL-Centric Dataset ^a	Linked Data ^a	62	72	67	67	56	61	91
OWL-Centric Dataset(90%) ^a	OWL-Centric Dataset(10%) ^a	79	72	75	74	81	77	80
OWL-Centric Dataset	OWL-Centric Test Set ^{ab}	58	68	62	62	50	54	58
OWL-Centric Dataset ^a	OWL-Centric Test Set ^{ab}	77	57	65	66	82	73	73
OWL-Centric Dataset	Synthetic Data ^a	70	51	40	47	52	38	51
OWL-Centric Dataset ^a	Synthetic Data ^a	67	23	25	52	80	62	50
Baseline								
OWL-Centric Dataset	Linked Data	73	98	83	94	46	61	43
OWL-Centric Dataset (90%)	OWL-Centric Dataset (10%)	84	83	84	84	84	84	82
OWL-Centric Dataset	OWL-Centric Test Set ^b	62	84	70	80	40	48	61
OWL-Centric Dataset	Synthetic Data	35	41	32	48	55	45	48

^a More Tricky Nos & Balanced Dataset

^b Completely Different Domain.

Table 3: Experimental results of proposed model

Experiments: Reasoning Depth



Test Dataset	Hop 0			Hop 1			Hop 2			Hop 3			Hop 4			Hop 5			Hop 6			Hop 7			Hop 8			Hop 9			Hop 10					
	P	R	F	P	R	F	P	R	F	P	R	F	P	R	F	P	R	F	P	R	F	P	R	F	P	R	F	P	R	F	P	R	F			
Linked Data ^a	0	0	0	80	99	88	89	97	93	77	98	86	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-
Linked Data ^b	2	0	0	82	91	86	89	98	93	79	100	88	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-
OWL-Centric ^c	19	5	9	31	75	42	78	80	78	48	47	44	4	34	6	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-
Synthetic	32	46	33	31	87	38	66	55	44	25	45	32	29	46	33	26	46	33	25	46	33	25	46	33	24	43	31	25	43	31	22	36	28			

^a LemonUby Ontology
^b Agrovoc Ontology
^c Completely Different Domain

Table 4: Experimental results over each reasoning hop

Dataset	Hop 1	Hop 2	Hop 3	Hop 4	Hop 5	Hop 6	Hop 7	Hop 8	Hop 9	Hop 10
<i>OWL-Centric</i> ^a	8%	67%	24%	0.01%	0%	0%	0%	0%	0%	0%
Linked Data ^b	31%	50%	19%	0%	0%	0%	0%	0%	0%	0%
Linked Data ^c	34%	46%	20%	0%	0%	0%	0%	0%	0%	0%
OWL-Centric ^d	5%	64%	30%	1%	0%	0%	0%	0%	0%	0%
Synthetic Data	0.03%	1.42%	1%	1.56%	3.09%	6.03%	11.46%	20.48%	31.25%	23.65%

^a Training Set
^b LemonUby Ontology
^c Agrovoc Ontology
^d Completely Different Domain

Table 5: Data distribution per knowledge graph over each reasoning hop

Training time: just over a full day

Generative RDFS Reasoning using Pointer Networks

Monireh Ebrahimi, breaking results

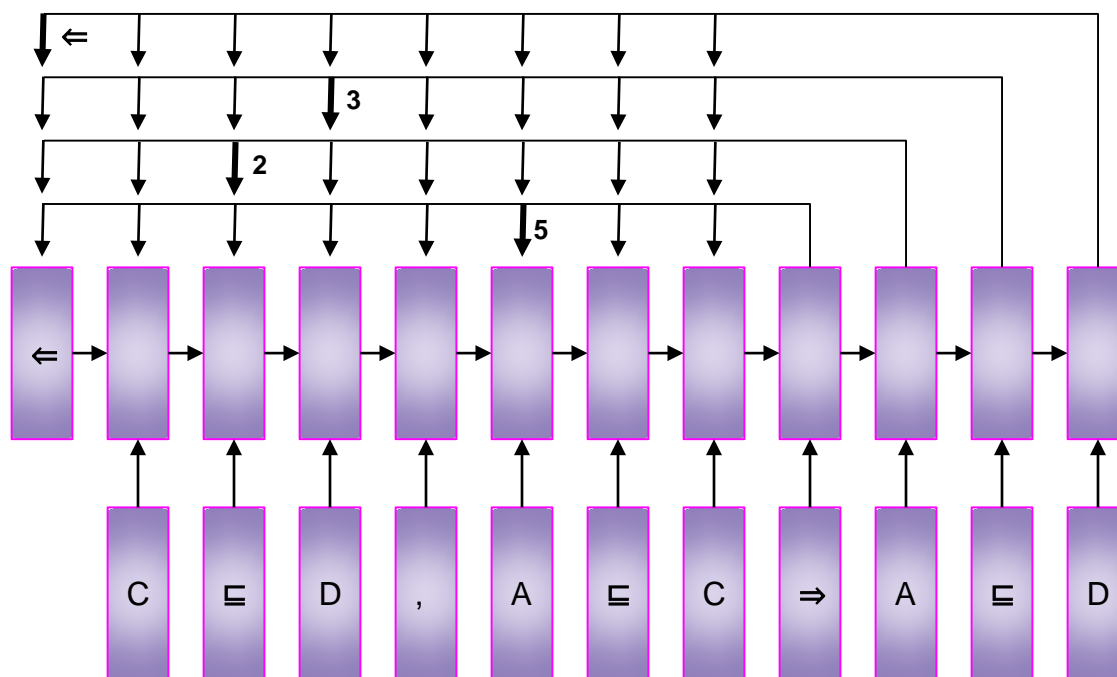


- **Pointer Networks ‘point’ to input elements!**
- **Ptr-Net approach specifically targets problems whose outputs are discrete and correspond to positions in the input.**
- **At each time step, the distribution of the attention is the answer!**
- **Application:**
 - **NP-hard Travelling Salesman Problem (TSP)**
 - **Delaunay Triangulation**
 - **Convex Hull**
 - **Text Summarization**
 - **Code completion**
 - **Dependency Parsing**

Pointer Networks for Reasoning



- To mimic human reasoning behaviour where one can learn to choose a set of symbols in different locations and copy these symbols to suitable locations to generate new logical consequences based on a set of predefined logical entailment rules



$$C \subseteq D, A \subseteq C \mapsto A \subseteq D$$

Preliminary Results



Logic	KG Size	Pointer Networks	
		SubWordText	Tokenizer
RDF	3 - 735	87%	99%
ER	40	73%	73%
	50	68%	68%
	120	49%	49%

- On RDF, slightly outperforms [Hendler Makni SWJ 2019] approach.
- Our approach is a more straightforward application.
- Evaluation is on the same dataset.

Completion Reasoning Emulation for the Description Logic EL+

Aaron Eberhart, Monireh Ebrahimi, Lu Zhou, Cogan Shimizu, Pascal Hitzler,
Completion Reasoning Emulation for the Description Logic EL+.
In: Andreas Martin, Knut Hinkelmann, Hans-Georg Fill, AURORA Gerber, Doug
Lenat, Reinhard Stolle, Frank van Harmelen (eds.), Proceedings of the
AAAI 2020 Spring Symposium on Combining Machine Learning and Knowledge
Engineering in Practice, AAAI-MAKE 2020, Palo Alto, CA, USA, March 23-25,
2020, Volume I.

EL+ is essentially OWL 2 EL



Table 2: \mathcal{EL}^+ Completion Rules

$CX \sqsubseteq CY$
$CX \sqcap CY \sqsubseteq CZ$
$CX \sqsubseteq \exists RY.CZ$
$\exists RX.CY \sqsubseteq CZ$
$RX \sqsubseteq RY$
$RX \circ RY \sqsubseteq RZ$

(1)	$A \sqsubseteq C$	$C \sqsubseteq D$	$\models A \sqsubseteq D$
(2)	$A \sqsubseteq C_1$	$A \sqsubseteq C_2$	$C_1 \sqcap C_2 \sqsubseteq D \models A \sqsubseteq D$
(3)	$A \sqsubseteq C$	$C \sqsubseteq \exists R.D$	$\models A \sqsubseteq \exists R.D$
(4)	$A \sqsubseteq \exists R.B$	$B \sqsubseteq C$	$\exists R.C \sqsubseteq D \models A \sqsubseteq D$
(5)	$A \sqsubseteq \exists S.D$	$S \sqsubseteq R$	$\models A \sqsubseteq \exists R.D$
(6)	$A \sqsubseteq \exists R_1.C$	$C \sqsubseteq \exists R_2.D$	$R_1 \circ R_2 \sqsubseteq R \models A \sqsubseteq \exists R.D$

Table 1: \mathcal{EL}^+ Semantics

Description	Expression	Semantics
Individual	a	$a \in \Delta^{\mathcal{I}}$
Top	\top	$\Delta^{\mathcal{I}}$
Bottom	\perp	\emptyset
Concept	C	$C^{\mathcal{I}} \subseteq \Delta^{\mathcal{I}}$
Role	R	$R^{\mathcal{I}} \subseteq \Delta^{\mathcal{I}} \times \Delta^{\mathcal{I}}$
Conjunction	$C \sqcap D$	$C^{\mathcal{I}} \cap D^{\mathcal{I}}$
Existential Restriction	$\exists R.C$	$\{ a \mid \text{there is } b \in \Delta^{\mathcal{I}} \text{ such that } (a, b) \in R^{\mathcal{I}} \text{ and } b \in C^{\mathcal{I}} \}$
Concept Subsumption	$C \sqsubseteq D$	$C^{\mathcal{I}} \subseteq D^{\mathcal{I}}$
Role Subsumption	$R \sqsubseteq S$	$R^{\mathcal{I}} \subseteq S^{\mathcal{I}}$
Role Chain	$R_1 \circ \dots \circ R_n \sqsubseteq R$	$R_1^{\mathcal{I}} \circ \dots \circ R_n^{\mathcal{I}} \subseteq R^{\mathcal{I}}$

with \circ signifying standard binary composition

Support



	New Fact	Rule	Support
Step 1	$C1 \sqsubseteq C3$	(1)	$C1 \sqsubseteq C2, C2 \sqsubseteq C3$
	$C1 \sqsubseteq C4$	(4)	$C1 \sqsubseteq C2, C1 \sqsubseteq \exists R1.C1, \exists R1.C2 \sqsubseteq C4$
	$C1 \sqsubseteq \exists R1.C3$	(3)	$C1 \sqsubseteq C2, C2 \sqsubseteq \exists R1.C3$
	$C1 \sqsubseteq \exists R2.C1$	(5)	$C1 \sqsubseteq \exists R1.C1, R1 \sqsubseteq R2$
	$C1 \sqsubseteq \exists R4.C4$	(6)	$C1 \sqsubseteq \exists R1.C1, R1 \circ R3 \sqsubseteq R4, C1 \sqsubseteq \exists R3.C4$
Step 2	$C1 \sqsubseteq C5$	(2)	$C3 \sqcap C4 \sqsubseteq C5, C1 \sqsubseteq C2, C2 \sqsubseteq C3, C1 \sqsubseteq C2, C1 \sqsubseteq \exists R1.C1, \exists R1.C2 \sqsubseteq C4$

Architecture

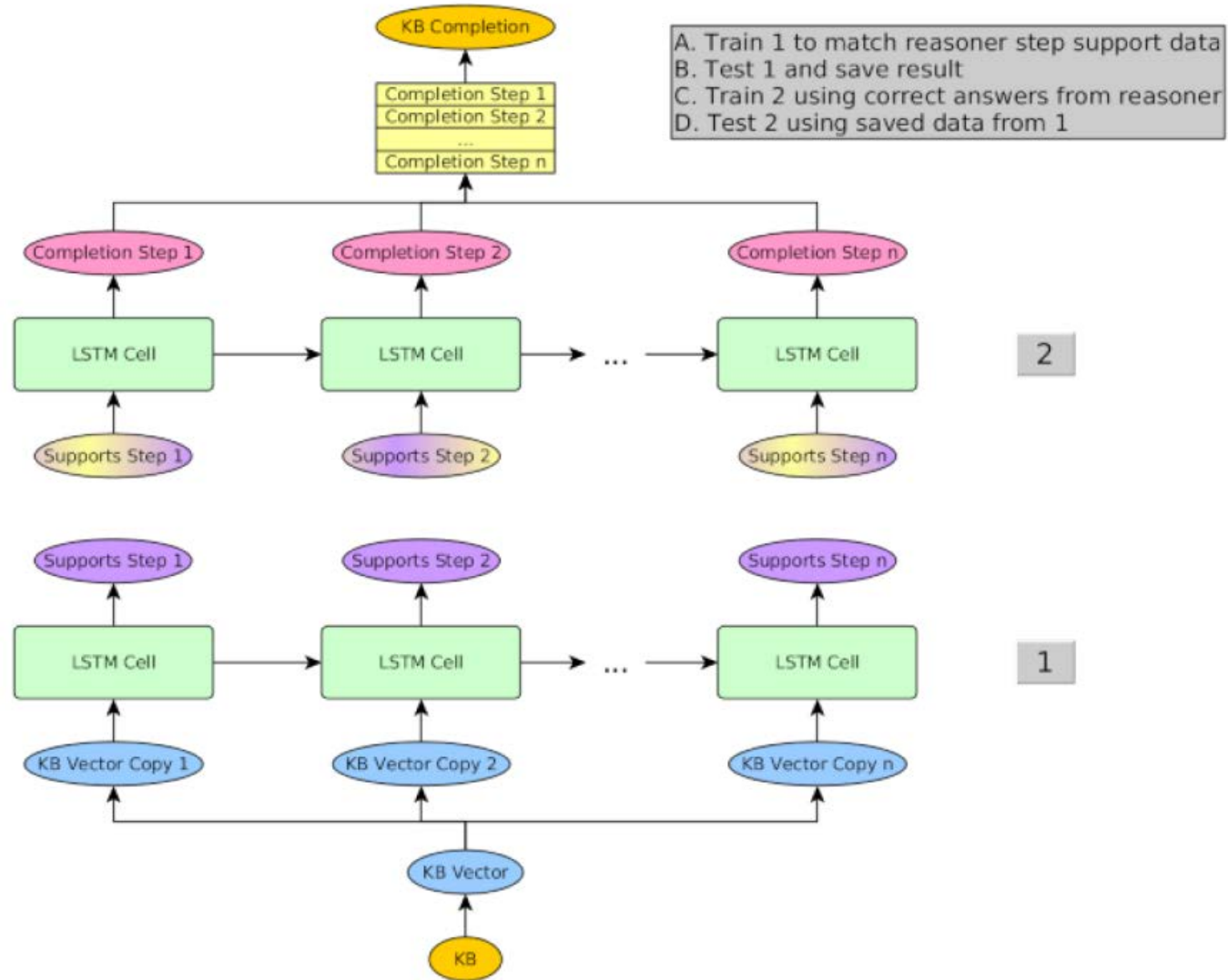


Figure 2: Piecewise Architecture

Architecture

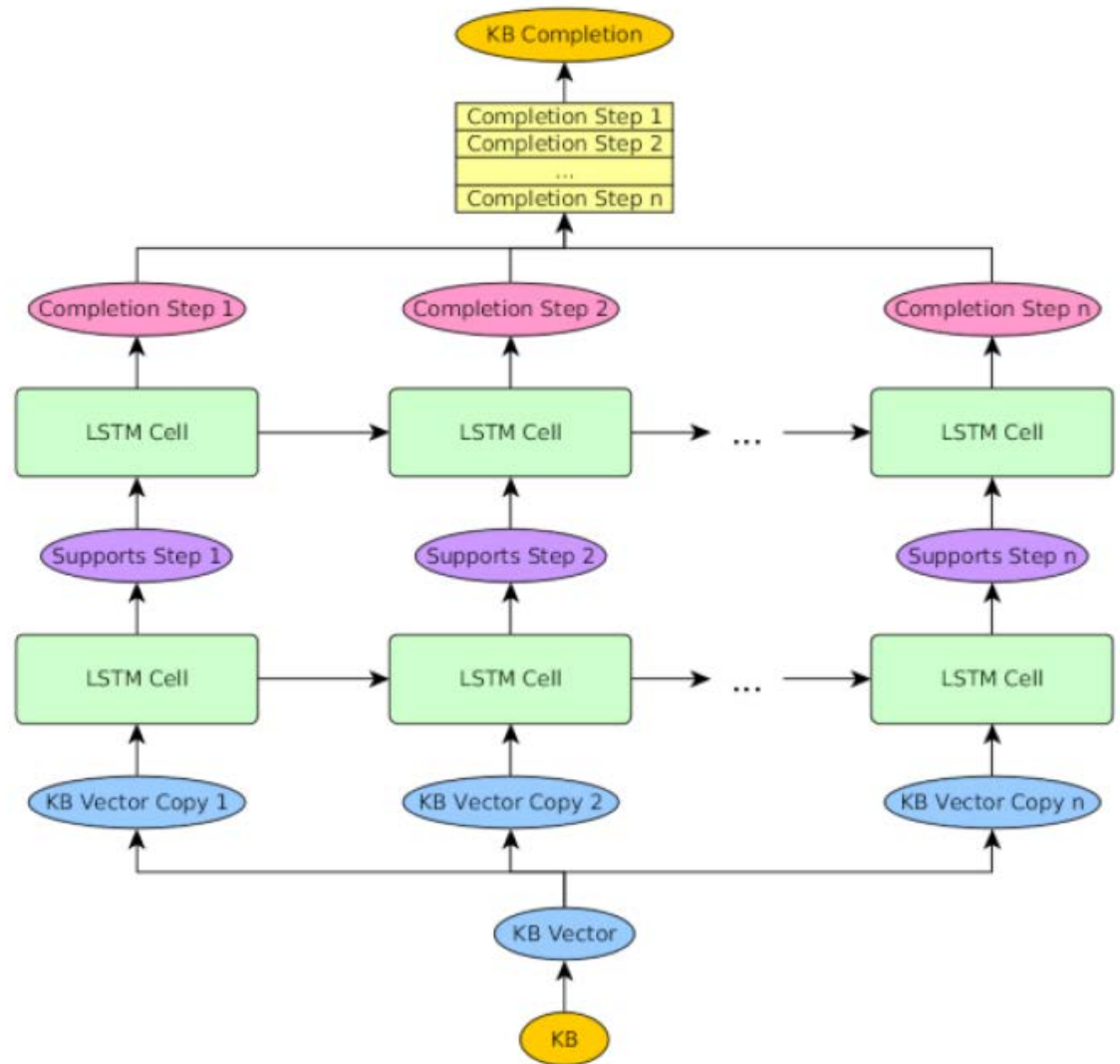


Figure 3: Deep Architecture

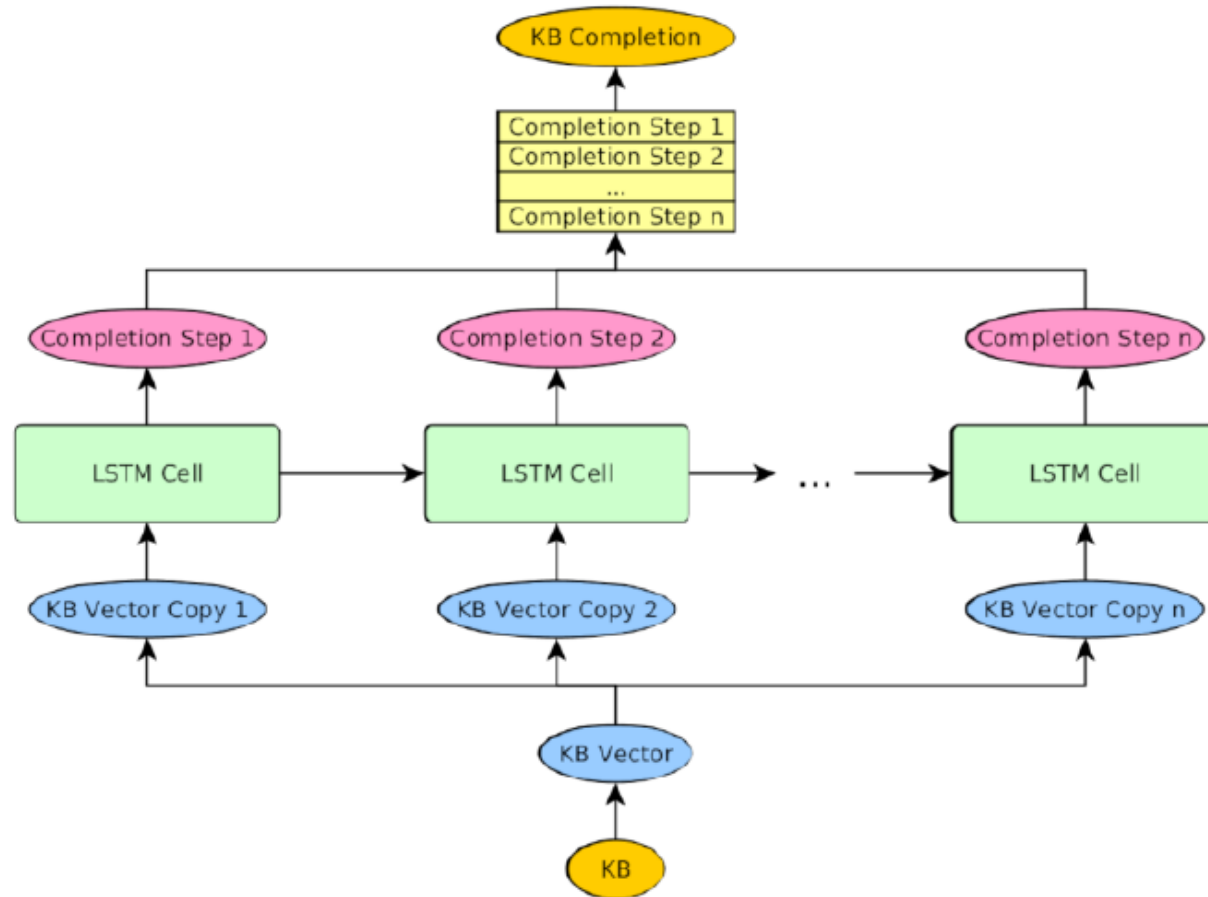


Figure 4: Flat Architecture

KB statement		Vectorization
$CX \sqsubseteq CY$	\rightarrow	$[0.0, \frac{X}{c}, \frac{Y}{c}, 0.0]$
$CX \sqcap CY \sqsubseteq CZ$	\rightarrow	$[\frac{X}{c}, \frac{Y}{c}, \frac{Z}{c}, 0.0]$
$CX \sqsubseteq \exists RY.CZ$	\rightarrow	$[0.0, \frac{X}{c}, \frac{-Y}{r}, \frac{Z}{c}]$
$\exists RX.CY \sqsubseteq CZ$	\rightarrow	$[\frac{-X}{r}, \frac{Y}{c}, \frac{Z}{c}, 0.0]$
$RX \sqsubseteq RY$	\rightarrow	$[0.0, \frac{-X}{r}, \frac{-Y}{r}, 0.0]$
$RX \circ RY \sqsubseteq RZ$	\rightarrow	$[\frac{-X}{r}, \frac{-Y}{r}, \frac{-Z}{r}, 0.0]$

c = Number of Possible Concept Names

r = Number of Possible Role Names

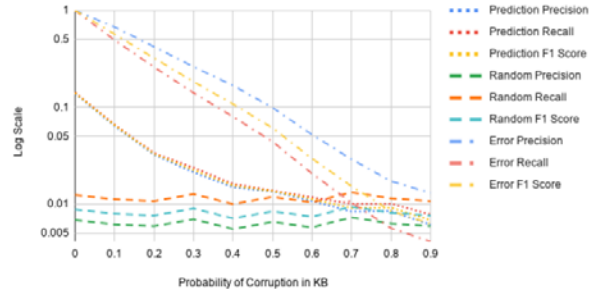
Table 7: Average Precision Recall and F1-score For each Distance Evaluation

	Atomic Levenshtein Distance			Character Levenshtein Distance			Predicate Distance		
	Precision	Recall	F1-score	Precision	Recall	F1-score	Precision	Recall	F1-score
	Synthetic Data								
Piecewise Prediction	0.138663	0.142208	0.140412	0.138663	0.142208	0.140412	0.138646	0.141923	0.140264
Deep Prediction	0.154398	0.156056	0.155222	0.154398	0.156056	0.155222	0.154258	0.155736	0.154993
Flat Prediction	0.140410	0.142976	0.141681	0.140410	0.142976	0.141681	0.140375	0.142687	0.141521
Random Prediction	0.010951	0.0200518	0.014166	0.006833	0.012401	0.008811	0.004352	0.007908	0.007908
	SNOMED Data								
Piecewise Prediction	0.010530	0.013554	0.011845	0.010530	0.013554	0.011845	0.010521	0.013554	0.011839
Deep Prediction	0.015983	0.0172811	0.016595	0.015983	0.017281	0.016595	0.015614	0.017281	0.016396
Flat Prediction	0.014414	0.018300	0.016112	0.0144140	0.018300	0.016112	0.013495	0.018300	0.015525
Random Prediction	0.002807	0.006803	0.003975	0.001433	0.003444	0.002023	0.001769	0.004281	0.002504

Noisy data

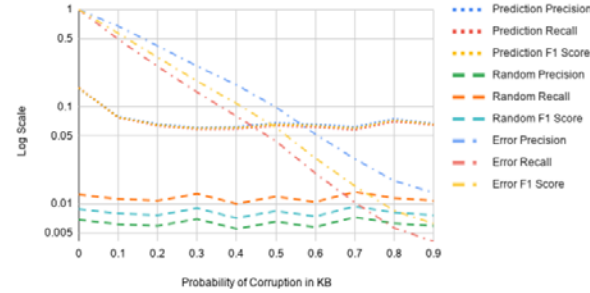


Averages For Levenshtein Distance



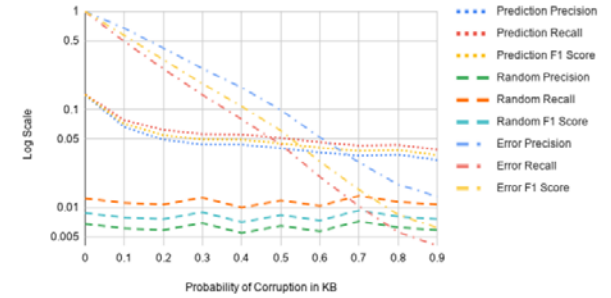
(a) Synthetic Data Piecewise Architecture

Averages For Levenshtein Distance



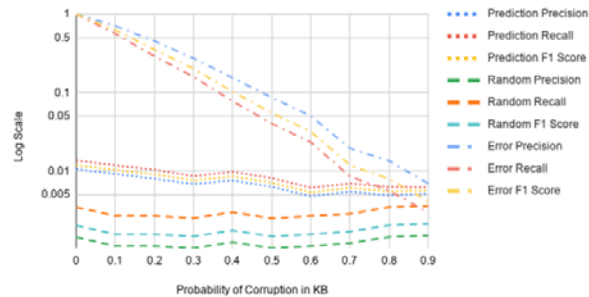
(b) Synthetic Data Deep Architecture

Averages for Levenshtein Distances



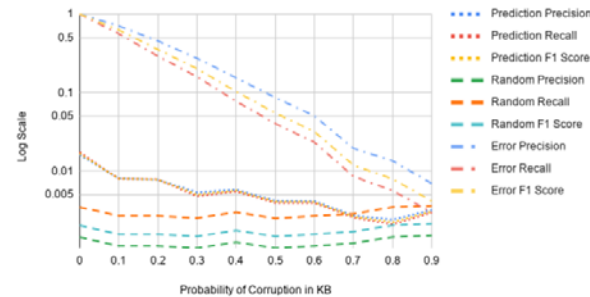
(c) Synthetic Data Flat Architecture

Averages for Levenshtein Distances



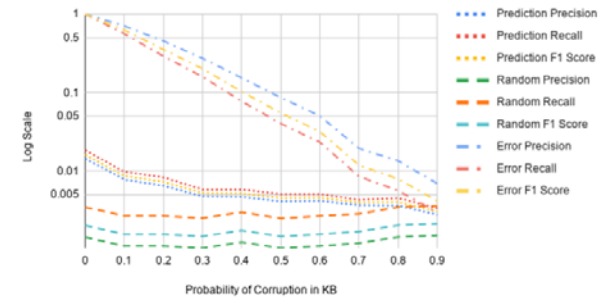
(d) SNOMED Data Piecewise Architecture

Averages for Levenshtein Distances



(e) SNOMED Data Deep Architecture

Averages for Levenshtein Distances



(f) SNOMED Data Flat Architecture

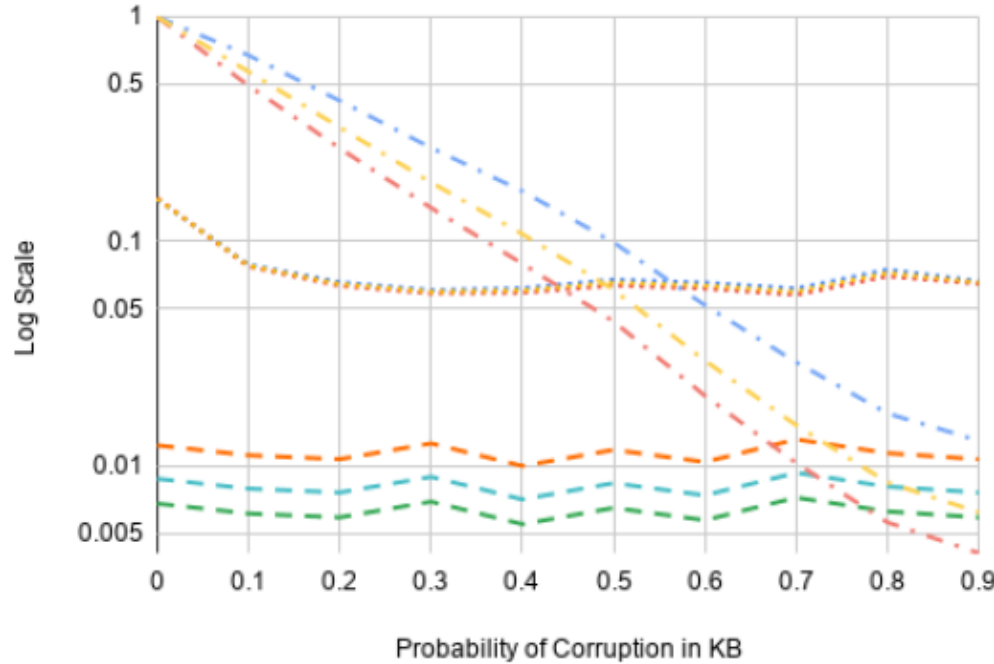
Figure 8: Character Levenshtein Distance Precision, Recall, and F1-score

Noisy data



Averages For Levenshtein Distance

- Prediction Precision
- Prediction Recall
- Prediction F1 Score
- Random Precision
- Random Recall
- Random F1 Score
- Error Precision
- Error Recall
- Error F1 Score



- Prediction Precision
- Prediction Recall
- Prediction F1 Score
- Random Precision
- Random Recall
- Random F1 Score
- Error Precision
- Error Recall
- Error F1 Score

Average

- Prediction Precision
- Prediction Recall
- Prediction F1 Score
- Random Precision
- Random Recall
- Random F1 Score
- Error Precision
- Error Recall
- Error F1 Score

hitecture

(b) Synthetic Data Deep Architecture

(c)

Averages for Levenshtein Distances

- Prediction Precision
- Prediction Recall
- Prediction F1 Score



- Prediction Precision
- Prediction Recall
- Prediction F1 Score

Average

- Prediction Precision
- Prediction Recall
- Prediction F1 Score

The Deductive Capability of Logic Tensor Networks

Federico Bianchi, Pascal Hitzler, On the Capabilities of Logic Tensor Networks for Deductive Reasoning. In: Andreas Martin et al. (eds.), Proceedings of the AAI 2019 Spring Symposium on Combining Machine Learning with Knowledge Engineering (AAAI-MAKE 2019) Stanford University, Palo Alto, California, USA, March 25-27, 2019, Stanford University, Palo Alto, California, USA, March 25-27, 2019. CEUR Workshop Proceedings 2350, CEUR-WS.org 2019.

Logic Tensor Networks



Based on Neural Tensor Networks.

Logic Tensor Networks are due to Serafini and Garcez (2016). They have been used for image analysis under background knowledge.

Their capabilities for deductive reasoning have not been sufficiently explored.

Underlying logic: First-order predicate, fuzzyfied.

Every language primitive becomes a vector/matrix/tensor.

Terms/Atoms/Formulas are embedded as corresponding tensor/matrix/vector multiplications over the primitives.

Embeddings of primitives are learned s.t. the truth values of all formulas in the given theory are maximized.

A-priori Limitations



- **Not clear how to adapt this such that you can transfer to unseen input theories.**
- **Scalability is an issue.**
- **While apparently designed for deductive reasoning, the inventors hardly report on this issue.**

Transitive closure



- $\forall a, b, c \in A : (sub(a, b) \wedge sub(b, c)) \rightarrow sub(a, c)$
- $\forall a \in A : \neg sub(a, a)$
- $\forall a, b : sub(a, b) \rightarrow \neg sub(b, a)$

Satisfiability	MAE	Matthews	F1	Precision	Recall
0.99	0.12 (0.12)	0.58 (0.45)	0.64 (0.51)	0.60 (0.47)	0.68 (0.55)
0.56	0.51 (0.52)	0.09 (0.06)	0.27 (0.20)	0.20 (0.11)	0.95 (0.93)
Random	0.50 (0.50)	0.00 (0.00)	0.22 (0.17)	0.14 (0.10)	0.50 (0.50)

parentheses: only newly entailed part of KB

MAE: mean absolute error;

Matthews: Matthews coefficient (for unbalanced classes)

top: top performing model, layer size and embeddings: 20, mean aggregator

Bottom: one of the worst performing models.

Multi-hop inferences difficult.

More take-aways from experiments



- Higher arity of predicates significantly increases learning time.

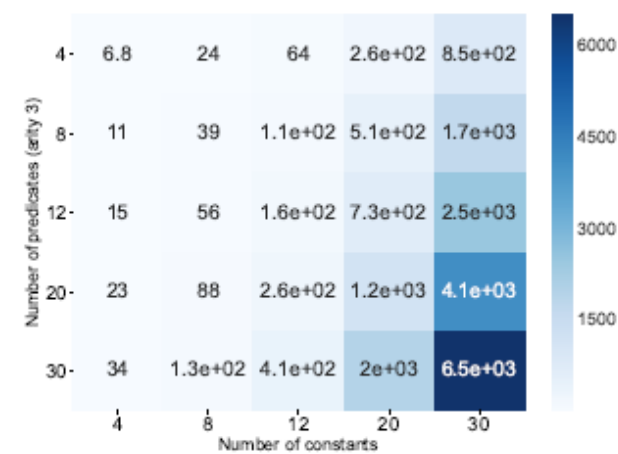
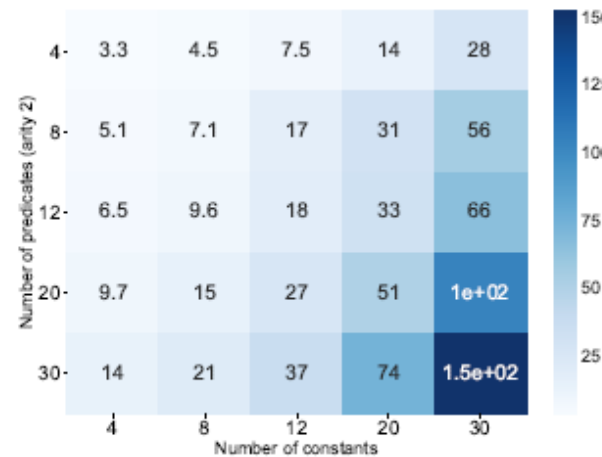
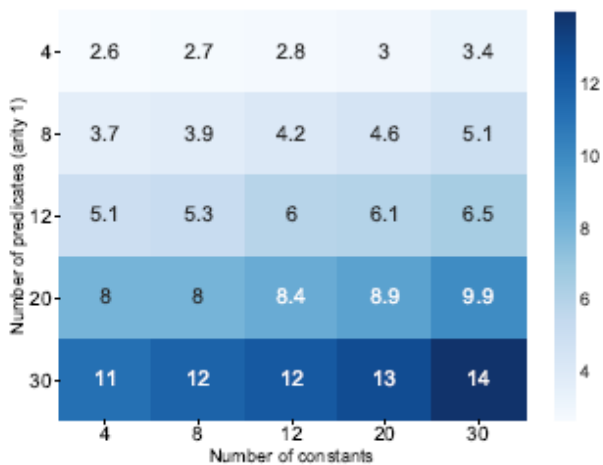


Figure 5: Computational times in seconds for predicates of arity one and constants

Figure 6: Computational times in seconds for predicates of arity two and constants

Figure 7: Computational times in seconds for predicates of arity three and constants

Part I: Deep Deductive Reasoners

Part 2: Explainable AI using Knowledge Graphs



Explaining Deep Learning via Symbolic Background Knowledge

Md. Kamruzzaman Sarker, Ning Xie, Derek Doran, Michael Raymer, Pascal Hitzler, Explaining Trained Neural Networks with Semantic Web Technologies: First Steps. In: Tarek R. Besold, Artur S. d'Avila Garcez, Isaac Noble (eds.), Proceedings of the Twelfth International Workshop on Neural-Symbolic Learning and Reasoning, NeSy 2017, London, UK, July 17-18, 2017. CEUR Workshop Proceedings 2003, CEUR-WS.org 2017

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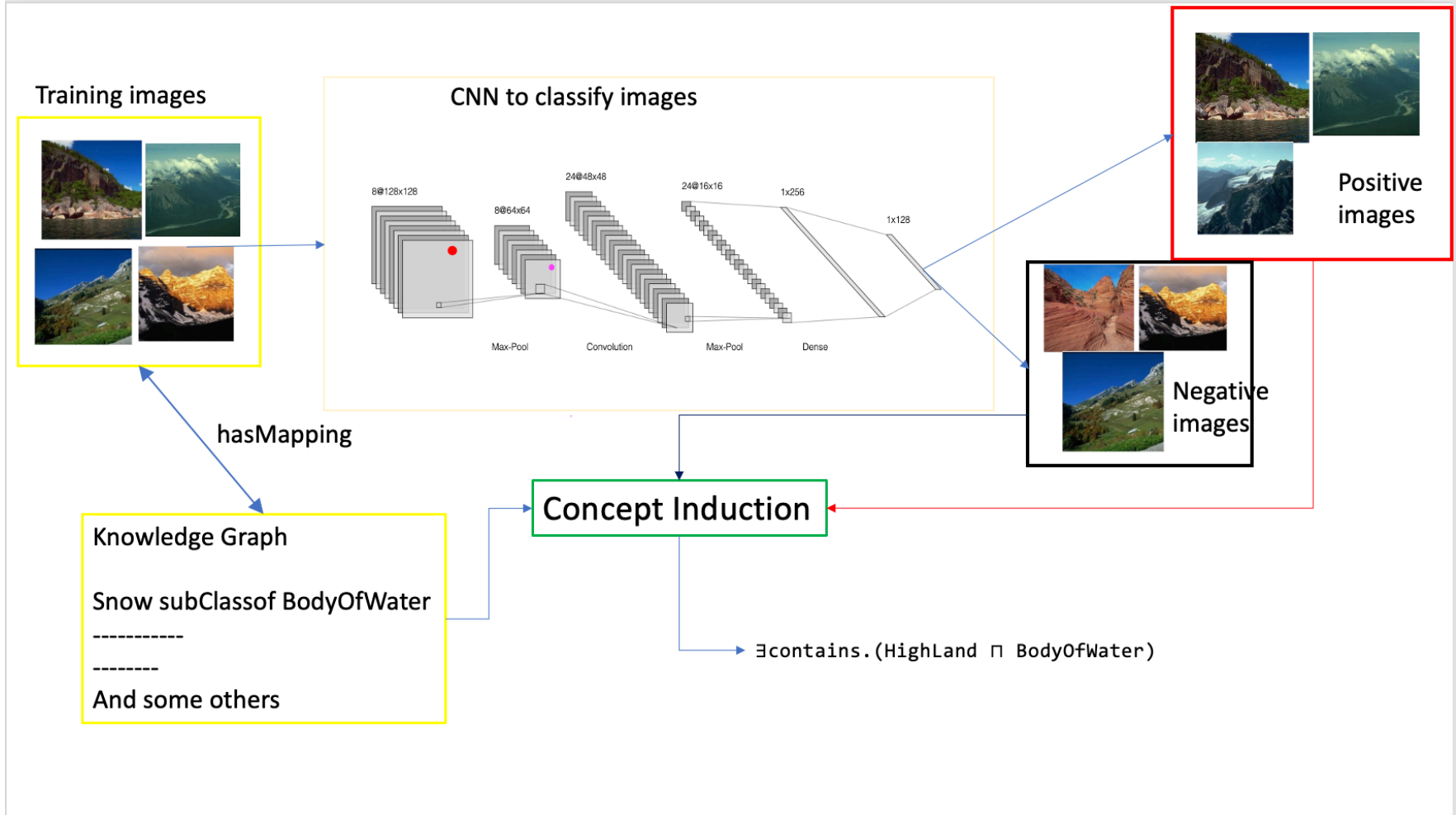
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Explainable AI



- **Explain behavior of trained (deep) NNs.**
- **Idea:**
 - **Use background knowledge in the form of linked data and ontologies to help explain.**
 - **Link inputs and outputs to background knowledge.**
 - **Use a symbolic learning system to generate an explanatory theory.**
- **We have key components for this now, but it's still early stages.**

Concept



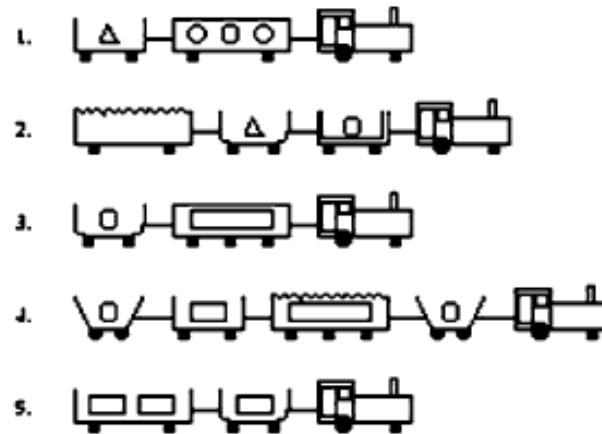
Concept Induction



Positive examples:



negative examples:



DL-Learner result:

$\exists \text{hasCar.}(\text{Closed} \sqcap \text{Short})$

In FOL:

$\{x \mid \exists y(\text{hasCar}(x, y) \wedge \text{Closed}(y) \wedge \text{Short}(y))\}$

ECII algorithm and system



- For scalability, we implemented our own system, **ECII (Efficient Concept Induction from Instances)** which trades some correctness for speed. **[Sarker, Hitzler, AAI-19]**

Experiment Name	Number of Logical Axioms	Runtime (sec)					Accuracy (α_1)		Accuracy α_2			
		DL ^a	DL FIC(1) ^b	DL FIC(2) ^c	ECII DF ^d	ECII KCT ^e	DL ^a	ECII DF ^d	DL FIC(1) ^b	DL FIC(2) ^c	ECII DF ^d	ECII KCT ^e
Yinyang_examples	157	0.065	0.0131	0.019	0.089	0.143	1.000	0.610	1.000	1.000	0.799	1.000
Trains	273	0.01	0.020	0.047	0.05	0.095	1.000	1.000	1.000	1.000	1.000	1.000
Forte	341	2.5	1.169	6.145	0.95	0.331	0.965	0.642	0.875	0.875	0.733	1.000
Poker	1,368	0.066	0.714	0.817	1	0.281	1.000	1.000	0.981	0.984	1.000	1.000
Moral Reasoner	4,666	0.1	3.106	4.154	5.47	6.873	1.000	0.785	1.000	1.000	1.000	1.000
ADE20k I	4,714	577.3 ^f	4.268	31.887	1.966	23.775	0.926	0.416	0.263	0.814	0.744	1.000
ADE20k II	7,300	983.4 ^f	16.187	307.65	20.8	293.44	1.000	0.673	0.413	0.413	0.846	0.900
ADE20k III	12,193	4,500 ^g	13.202	263.217	51	238.8	0.375	0.937	0.375	0.375	0.930	0.937
ADE20k IV	47,468	4,500 ^g	93.658	523.673	116	423.349	0.375	NA	0.608	0.608	0.660	0.608

^a DL : DL-Learner

^b DL FIC (1) : DL-Learner fast instance check with runtime capped at execution time of ECII DF

^c DL FIC (2) : DL-Learner fast instance check with runtime capped at execution time of ECII KCT

^d ECII DF : ECII default parameters

^e ECII KCT : ECII keep common types and other default parameters

^f Runtimes for DL-Learner were capped at 600 seconds.

^g Runtimes for DL-Learner were capped at 4,500 seconds.

ECII vs. DL-Learner

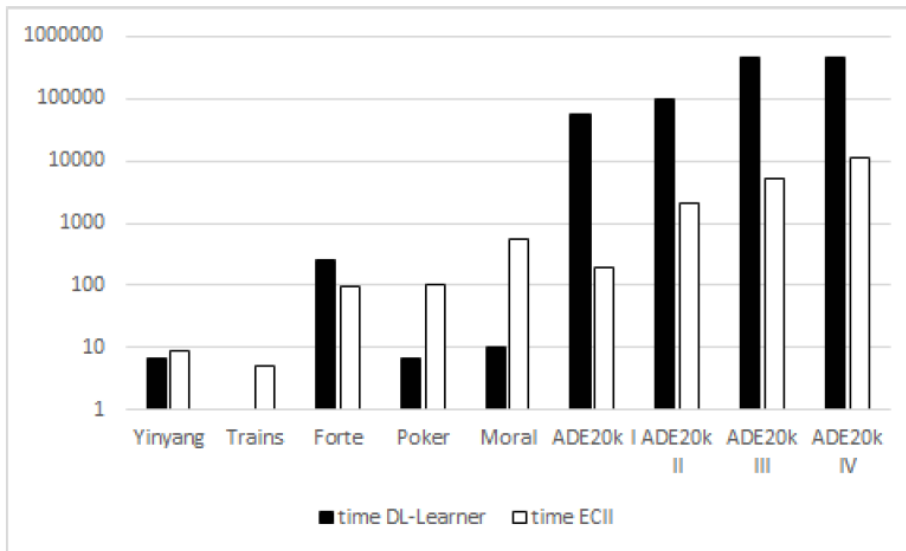


Figure 1: Runtime comparison between DL-Learner and ECII. The vertical scale is logarithmic in hundredths of seconds, and note that DL-Learner runtime has been capped at 4,500 seconds for ADE20k III and IV. For ADE20k I it was capped at each run at 600 seconds.

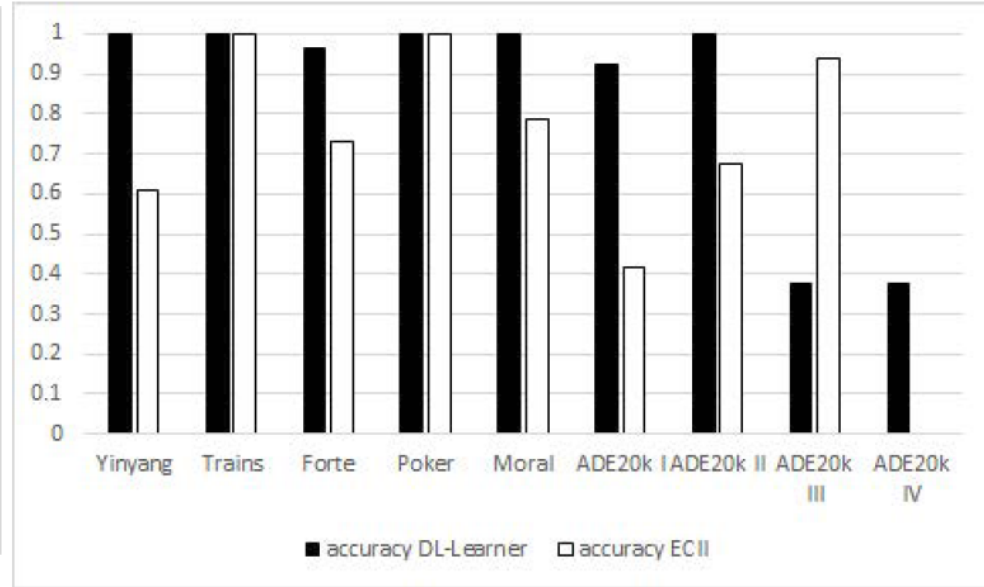


Figure 2: Accuracy (α_3) comparison between DL-Learner and ECII. For ADE20k IV it was not possible to compute an accuracy score within 3 hours for ECII as the input ontology was too large.

However, ECII can only deal with class hierarchies as background knowledge.

Proof of Concept Experiment



Positive:



Negative:



Come from the MIT ADE20k dataset

<http://groups.csail.mit.edu/vision/datasets/ADE20K/>

They come with annotations of objects in the picture.

We mapped these to SUMO as background knowledge.

- Suggested Merged Upper Ontology**
- Approx. 25,000 common terms covering a wide range of domains**

DL-Learner input



Positive:

img1: road, window, door, wheel, sidewalk, truck, box, building

img2: tree, road, window, timber, building, lumber

img3: hand, sidewalk, clock, steps, door, face, building, window, road

Negative:

img4: shelf, ceiling, floor

img5: box, floor, wall, ceiling, product

img6: ceiling, wall, shelf, floor, product

DL-Learner results include:

\exists contains.Transitway

\exists contains.LandArea

Proof of Concept Experiment



Positive:



Negative:



Contains Transitway

Contains Land Area

Experiment 5



Positive:



Negative (selection):



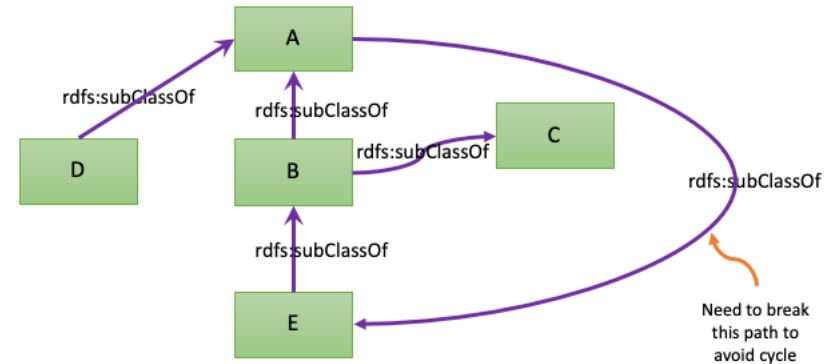
\exists contains.BodyOfWater

Wikipedia KG (WKG) : Breaking Cycle



Lost Significant Information

- 50% of the subclass relation
- 50% of the class assertion



Number of entities/facts	SUMO	DBpedia	Wikipedia cyclic	Wikipedia noncyclic
Concepts	4558	1183	1,901,708	1,860,342
Individuals	86,475	1	6,145,050	6,079,748
Object property	778	1144	2	2
Data property	0	1769	0	0
Axioms	175,208	7228	71,344,252	39,905,216
Class assertion axioms	167381	1	57,335,031	27,991,282
Subclass axioms	5330	769	5,962,463	3,973,845

Evaluation : Knowledge Graph in XAI

e Lab

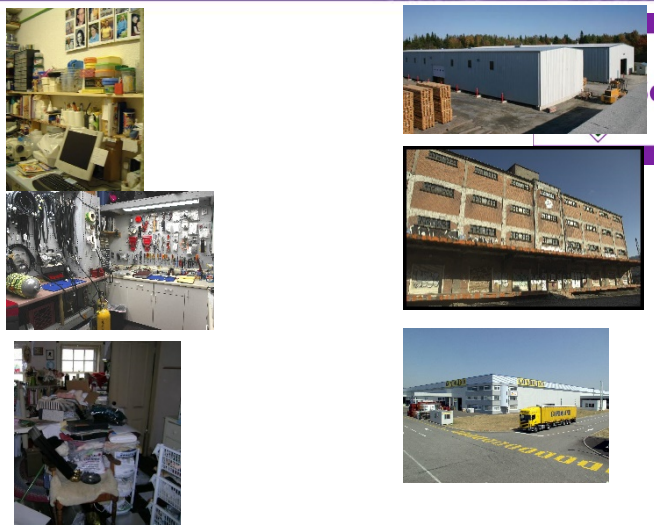
Workroom Explanations

SUMO

- $\exists \text{contains.}(\text{DurableGood} \sqcap \neg \text{ForestProduct})$
- $\exists \text{contains.}(\text{DurableGood} \sqcap \neg \text{Lumber})$
- $\exists \text{contains.} \text{Entity}$

Wikipedia

- $\exists \text{contains.}(\text{Wrenches} \sqcap \text{Tools} \sqcap \neg \text{Lumber})$
- $\exists \text{contains.}(\text{Mechanicaltools} \sqcap \neg \text{Lumber})$
- $\exists \text{contains.}(\text{Mechanicaltools} \sqcap \neg \text{Sky})$



Test images. **Workroom** as positive examples p_1, p_2, p_3 on the left, **Warehouse** as negative examples n_1, n_2, n_3 on the right (from top).

Market Explanations

SUMO

- $\exists \text{contains.} \text{SentientAgent}$

Wikipedia

- $\exists \text{contains.}(\text{Structure} \sqcap \text{Life})$

Mountain Explanations

SUMO

- $\exists \text{contains.} \text{BodyOfWater}$

Wikipedia

- $\text{contains.}((\text{Life} \sqcap \text{Branches_of_botany}) \sqcap (\text{Nature}))$



Evaluation : Knowledge Graph in XAI

- Wikipedia Knowledge graph producing better coverage score.
 - Reason behind this is the large number of concepts it has.

Experiment name	#Images	#Positive images	Wikipedia		SUMO	
			#Solution	Coverage	#Solution	Coverage
Market vs. WorkRoom and wareHouse	96	37	286	.72	240	.72
Mountain vs. Market and workRoom	181	85	195	.61	190	.53
OutdoorWarehouse vs. IndoorWarehouse	55	3	128	.94	102	.89
Warehouse vs. Workroom	59	55	268	.56	84	.24
Workroom vs. Warehouse	59	4	128	.93	93	.84

Future Work



- **Use approach to identify meaning of hidden neurons.**
- **Use approach to improve deep learning systems.**
- **Applications to understand “data differences”.**
E.g., false-positives vs. true-positives.

Conclusions

Conclusions



- **Bridging the neural-symbolic gap is still a major quest.**
- **But there are tons of opportunities.**



Thanks!

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Thanks!